

ON THE LOCAL INTERACTION OF MONEY AND CREDIT¹

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Abstract

We study the coexistence of monetary and credit transactions in a model where exchange is decentralized. Agents belong to different villages which are informationally separated. The equilibrium mix of monetary and credit transactions is characterized as a function of the frequency of meetings among agents from different villages. Our economy may be interpreted as a medieval economy. Trade takes place only among a small set of nearby villages via the use of credit. Monetary trades might emerge only if interactions with faraway villages are sufficiently frequent. Even in that case, trades among nearby villages remain non-monetized.

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1. INTRODUCTION

In many situations throughout history, we observe that people use credit with people that they meet frequently, while they use money in trades with people that they meet infrequently. In this paper, we capture the coexistence of such monetary and credit transactions in a model where trade is decentralized.

Our analysis is motivated by observations from transactions in medieval village economies. In some cases these villages were largely closed, non-market economies.² In his study of markets in England and Wales between the years 1200-1500, David L. Farmer refers to ... a network of lending and borrowing among acquaintances, mainly for small amounts, [which] could well strengthen the social fabric of a village with a fairly static population. It could not serve in the same way an international fair, a port, or even a major market town, where litigants could not wait for the next regular borough court to press their pleas.³ As mobility increased, so did the frequency of interactions with outsiders, and monetary transactions became commonplace. Still, at least in some cases, trades among people from the same or neighboring villages remained largely non-monetized for a long time.

We build a model based on the work of Kiyotaki and Wright (1989). The decentralized way in which goods and information are exchanged in this model makes it appropriate for the study of issues concerning early economies in which centralized markets were scarce or non-existent. We add two features to the standard setup. First, matching is not uniform but local. That is, people from the same (or neighboring) villages are more likely to meet each other than people from faraway places. Second, public record-keeping of agents' trading histories is available only within their

²For example, there seems to have been little commercial exchange and no markets in Wales before 1066 (see Thirsk (1991), page 332). Townsend (1993) provides a detailed analysis of the medieval village economy.

³See Thirsk (1991), page 423.

village.

We begin by studying conditions that guarantee that trade takes place only among agents from nearby villages and only via the use of credit. In this case, money has no possible welfare-improving role. Monetary trades might emerge only when interactions with faraway villages become sufficiently frequent. In that case, both means of payment coexist. Credit is used in trades among neighbors, whereas money is used in trades among strangers.⁴

The idea that credit-like instruments are used in trades among agents with known histories while currency is used in trades among relative strangers is not new. Townsend (1989), for example, studies a model in which both types of transactions coexist and are essential to support efficient outcomes. In his model, as in ours, money and credit differ in their communication and record-keeping aspects. In earlier work Lucas (1980) suggested that a friction involved in establishing one's creditworthiness might lead to the coexistence of money and credit transactions since, in that case, money will economize on record-keeping costs. This distinction is also present in Prescott (1987), who studied a model with transaction costs in which a form of bank drafts is used for large transactions while currency is used for small ones. In his model, the use of monetary transactions can be thought of as a way to economize on costly information collection regarding agents' trading histories. In our model, money is shown to be essential for facilitating trade among agents that meet infrequently and do not have access to information about each other's trading histories. One contribution of our paper is to characterize conditions under which a random matching model is consistent with the above observations.

Our work is also related to a number of papers that study credit in a search-based setup starting with Diamond (1990). Kranton (1996) studied the sustainability of

⁴Our analysis is mainly positive in the sense that we build a model that delivers this coexistence as an equilibrium outcome, and we largely abstract from normative issues.

reciprocal exchange. Shi (1996) and Corbae and Ritter (1997) study money and credit in a search setup. Unlike them, we do not allow pairs of agents to form ongoing relationships by staying together for more than one period. Kocherlakota and Wallace (1998) build on Kocherlakota (1998) and study the coexistence of money and credit in an environment where public record-keeping is incomplete because it is updated with a lag. Record-keeping is also incomplete in our model, but in the sense that it is available only locally.

It is worth mentioning that while here we concentrate on the implications of a local matching rule and of a locally available record-keeping technology for monetary theory, our setup might be useful in the study of other issues that involve local interactions. For example, search in labor markets often has a local feature, and reputation of certain goods and services is often available only locally.

The paper proceeds as follows. Section 2 offers an informal description of the model, and Section 3 describes the environment. Section 4 presents the benchmark case of uniform matching. Section 5 contains the main results. Section 6 concludes the paper. The Appendix contains the value functions and Figures.

2. AN INFORMAL DESCRIPTION OF THE MODEL

As certain aspects of our model are non-standard, we first describe the setup informally. In the standard random matching model, credit cannot exist since agents do not meet repeatedly, and there is no record-keeping of past trades. We amend the standard model in two ways: by assuming that agents meet different sets of agents with different probabilities, and by introducing record-keeping at the local level. Although other interpretations are possible, we interpret the different meeting probabilities as being the result of the agents' respective geographic distance from one another. Agents populate villages that are symmetric, each populated by a large number (a continuum) of agents. Agents are specialized in production and consump-

tion of goods and are assumed to be randomly matched in pairs in each period. Trade is possible in the case where a potential producer meets with someone that likes his production good (hence called a single-coincidence meeting). The distribution of all agents' characteristics is the same across villages. With high probability, each agent meets someone from his own village, and the probability of meeting another agent decreases as the distance from the village that the agent belongs to increases. In addition, we assume that each individual's trading history is public information only within the village where they belong, and only in regard to their meetings with agents from that village.

What are the likely methods of payment if trade occurs in this environment? One possibility is that producers offer to produce without requiring immediate payment in all single-coincidence meetings regardless of the location of the consumer. In the context of our model, we will identify such a non-monetized exchange with a credit transaction. Suppose that if one agent deviates from this implicit agreement, say by refusing to produce for someone from village j , the deviation triggers a collective punishment to permanent no-trade between the deviator and village j .⁵ One may think that the above threat might induce an equilibrium in which credit is used in all trades. However, consider an agent in a meeting with someone from a very faraway village. The potential producer has a strong incentive to deviate. The disutility of producing is suffered now, while the punishment will be borne sometime in the distant future.⁶ For sufficiently low discount factors, the producer will refuse to produce. Our main result establishes conditions for the existence of a critical distance (frequency of meetings) such that in a stationary equilibrium, only credit transactions take place among close neighbors (people whose frequency of meetings is higher than

⁵Later we discuss the sensitivity of our results to the exogenous specification of the punishment.

⁶This requires that the close neighbors of the deviating producer remain unaware of his deviation. Later we make assumptions that guarantee that this will be true in our setup.

a critical value), while only monetary transactions occur in meetings between people from faraway places (people whose frequency of meetings is lower than the critical value).

3. THE ENVIRONMENT

Time is discrete and the horizon is infinite. The economy is populated by a continuum of agents of measure 1. Agents are matched bilaterally in every period. There is an (odd) number of villages denoted by $j = 1, 2, \dots, n$, forming a partition of the unit circle with a continuum of agents in each village. There is a finite number, $k \geq 3$, of perishable and indivisible consumption goods. Agents specialize in consumption and production in a symmetric fashion. At the beginning of each period, there is a $[0, \frac{1}{k}]$ continuum of each type. Individuals of type i consume good i and produce good $i + 1$ (modulo k), where $i = 0, \dots, k - 1$. The instantaneous utility from consumption is $u > 0$. Production requires an effort that gives disutility $e > 0$, where $u > e$. Agents maximize expected discounted utility, and the time discount factor is $\beta \in (0, 1)$. Because $k \geq 3$, there is no double coincidence of wants. We assume that a fraction M of agents each start with one unit of indivisible, storable, and intrinsically useless fiat money. Current period money holdings are observable within a match. We impose an upper bound on individual holdings; i.e., individuals can hold at most one unit of currency or one unit of a good. This implies that, in meetings where there is monetary trade, one unit of money is exchanged for one unit of good.⁷ Agents are assigned to villages at the beginning of time. The initial distribution of all agents' characteristics, including money holdings, is uniform across consumption types and villages. We will concentrate on stationary perfect equilibria that respect this symmetry.

⁷The indivisibility assumption is largely for simplicity. Introducing endogenous prices as in Shi (1995) and Trejos and Wright (1995) would complicate our analysis without qualitatively changing the results.

Local Matching

One difference between the environment of our model and the standard setup in existing search models is in the matching technology. Matching here is not uniform but *local*. Each agent is matched with an agent from the same village with probability p_0 ; he is matched with an agent from either of the two immediately neighboring villages with probability p_1 , where $p_0 > p_1 > p_2 > \dots$, etc. There is no loss of generality in concentrating our analysis on a distinguished agent from a generic village, j . Denote by d the distance between our generic village and any other village, j' ; i.e., $d = |j - j'|$. Hence, p_d stands for the probability that our distinguished agent is matched with an agent from a d -order neighboring village, where $\sum_{d=0}^{\frac{n-1}{2}} p_d = 1$. Agents return to their village at the end of each period. We assume that the realizations of the matching probabilities are *perfectly correlated* across agents in the same village. In other words, if the random matching technology assigns one agent from village j to an agent from village j' , then each agent from village j is assigned to an agent from village j' in that period. The role of this assumption is explained later.

The Coordination Mechanism

Here we present our informational assumptions and describe the trading mechanism. A second novel feature of our model is that agents from different villages cannot exchange information regarding trading histories. This captures that, especially in early village economies, it was costly to have access to credit histories, and these costs increased as a function of distance.⁸

⁸One could argue that these costs are relevant even today. For example, it is easier to have access to the credit history of someone who lives in the same country than that of someone who lives overseas.

A potential deviation experienced by an agent from village j is automatically communicated to all agents in village j by the agent that experienced the deviation and triggers a punishment to permanent no trade with the deviating agent by all agents in village j .⁹ Of course, the deviator has no incentive to reveal that he deviated. Actions during meetings with agents from other villages are not publicly observable in the deviator's own village. The perfect correlation assumption in the matching technology ensures two features that are important for what follows: (1) information about trading histories remains local and (2) there is no aggregate uncertainty so that the model remains tractable.¹⁰

When two agents have a single-coincidence meeting, they simultaneously make a trading proposal after they observe each other's type, current money holdings, and village of origin. The potential consumer has three choices: (1) to request production offering no payment, (2) to offer money in exchange for production, and (3) to propose no trade. The producer also has three choices: (1) to offer to produce requesting no payment, (2) to request money in exchange for production, and (3) to propose no trade. If the two proposals match, the resulting trades are realized. If they are

⁹Following common practice, we assume that a deviation triggers a punishment to the worst reasonable equilibrium. In earlier versions of the paper we assumed that individuals cannot be recognized and the entire village of the deviator is punished. The results still hold in this case. The same is true if agents are punished to monetary exchange instead of autarky, although the notation in that case is cumbersome. In general, a lesser punishment requires a higher discount factor in order to maintain the same composition of credit and monetary trades. One important issue is whether such punishments are renegotiation-proof. While this will not be the case in general, we believe that they are for some parametrizations. Nevertheless, following the literature, we concentrate on unilateral deviations.

¹⁰If the probabilities were *i.i.d.*, as a result of the law of large numbers, positive fractions of agents from any village would meet with agents from all other villages. Thus, if one village was informed of a deviation and triggered *global* autarky, this could lead to global autarky two periods after the deviation occurred.

different, then a punishment is triggered.¹¹

Consider our distinguished agent in a meeting with an agent from a village that is d steps away. We denote by α^d the probability with which an agent requests money in exchange for production, and by m^d the probability that he offers money in order to consume. Similarly, let g_{M_p, M_c}^d and h_{M_p, M_c}^d be the respective probabilities that an agent produces requesting no payment and that he requests production offering no payment when the producer's and the consumer's money holdings are given by M_p and M_c , respectively. The remaining probability is assigned to the event that a no-trade proposal is made. To economize on notation, we surpass the dependence of these variables on the set of villages that, as a result of past deviations, are in the state of permanent no-trade with our agent.

Of course, the punishment to permanent no-trade is arbitrary, and one could think of several alternatives. The harshest possible punishment that a deviated-upon village could adopt is to revert to permanent autarky during all future meetings with all villages.¹² Even if this punishment is adopted, a long lag before it reaches the deviator guarantees that the qualitative properties of our results still hold. On the other hand, we could adopt the less harsh punishment of allowing monetary exchanges in future meetings with a known deviator.¹³ As we mentioned earlier, this would complicate

¹¹We shall ignore the case where the producer offers to produce requesting no payment while the consumer offers money. This, of course, would never occur in equilibrium. Our results hold if we assume that in such a case production takes place, regardless of whether money changes hands or not.

¹²This punishment defines one end of the spectrum, but it is unattractive. For example, agents in the deviated-upon village know the location of the deviator. It does not seem reasonable to punish themselves by adopting autarky in meetings within the village, or in meetings with their close neighbors, especially if the deviating agent's village is far away.

¹³This is especially relevant since both the deviator and his partner might have an incentive to perform a monetary exchange instead of making no proposals. However, notice that, given our mechanism, making no proposals in such a meeting remains *an* equilibrium. In fact, if we assume

the analysis without qualitatively changing the results.

The general value functions (A.1 and A.2) are provided in the Appendix. A symmetric perfect equilibrium consists of values for g_{M_p, M_c}^d , h_{M_p, M_c}^d , α^d and m^d that satisfy A.1 and A.2, and are such that $g_{M_p, M_c}^d = h_{M_p, M_c}^d$ and $\alpha^d = m^d$.

4. A BENCHMARK CASE - UNIFORM MATCHING

Our main focus is the study of a model where both record-keeping and matching are local. In order to separate the role of these two assumptions, we first consider the case where matching is uniform, while information about histories is available only at the local level. Suppose there are n villages and $p_d = p = \frac{1}{n}$, for all d . The following proposition asserts that in this environment, money and credit payments cannot coexist in a non-trivial way. More precisely, credit exchange across all meetings can be supported as an equilibrium outcome for low values of n , while credit exchange cannot be supported for high values of n .

Proposition 1 *Suppose that $\beta \in (0, 1)$. There is a unique n^* such that if $p \in (\frac{1}{n^*}, 1)$, there exists a pure credit equilibrium, and money is not essential. If $p \in (0, \frac{1}{n^*})$, there exists no equilibrium with credit transactions.*

The above follows as a Corollary of the main Proposition in the next section. The intuition is simple. A deviation from offering credit triggers permanent no-trade with the village of the deviated-upon agent. Producing implies a certain amount of disutility that the producer suffers today. On the other hand, the potential cost from the autarky punishment depends on the frequency with which the penalty is experienced in the future. If the probability of meeting the same village in the future is high enough, the best response is to offer credit. Otherwise, the best response will be to deviate. Since the meeting probabilities are equal, the result follows.

an arbitrarily small cost of making a proposal, it is a strict equilibrium.

5. MONEY AND CREDIT UNDER LOCAL MATCHING

In this section we derive our main proposition establishing conditions that guarantee the coexistence of monetary and credit transactions. We can think of the random matching technology as operating in two steps. First, a village is matched to any other, including itself, with some probability. The second step determines the individual agent matches. We first prove some preliminary results. The first Lemma asserts that the search economy in Kocherlakota (1998) follows as a special case of our setup if we shut down all meetings across different villages ($p_0 = 1$). In that case, each village is an isolated economy under uniform matching, and a high discount factor guarantees the existence of a credit equilibrium. No monetary arrangement can result in a higher frequency of consumption than the credit equilibrium. This is because in a credit equilibrium trade takes place in each single-coincidence meeting, while with money it is also needed that in at least some meetings the consumer has money and the producer does not. We will concentrate on the Pareto superior credit regime whenever such a regime can be supported between two villages.

Lemma 1 *Suppose that $p_0 = 1$. There exist β^C and β^M with $0 < \beta^C < \beta^M < 1$ such that for all $\beta \in (\beta^C, 1)$, a credit equilibrium exists, and for all $\beta \in (\beta^M, 1)$, a monetary equilibrium exists. Welfare in the credit equilibrium is strictly higher than in any equilibrium in which money is used.*

Proof: We let V^C be the value function under a credit regime, and we denote by V_1^M and V_0^M the value functions of a money holding and a non-money holding agent, respectively, under a monetary regime. In a credit equilibrium we have that $V^C = \frac{u-e}{k(1-\beta)} > 0$. In order for $g^d = 1$ to be the best response for a producer in a single coincidence meeting where $h^d = 1$, we need that $-e + \beta V^C \geq 0$, which implies that $\beta \geq \frac{ek}{ek+u-e} \equiv \beta^C$. On the other hand, since $u + \beta V^C > 0$, we have that $h^d = 1$ is

the best response given $g^d = 1$. That is, the credit equilibrium exists provided that $\beta \in (\beta^C, 1)$. In a monetary equilibrium we have

$$V_1^M = \frac{1}{k} (1 - M) \left(u + \beta V_0^M \right) + \left[1 - \frac{1}{k} (1 - M) \right] \beta V_1^M \quad (1)$$

$$V_0^M = \frac{1}{k} M \left(-e + \beta V_1^M \right) + \left(1 - \frac{1}{k} M \right) \beta V_0^M. \quad (2)$$

For a monetary equilibrium to exist, we need that $-e + \beta V_1^M \geq \beta V_0^M$. Solving for V_0^M and V_1^M and substituting, we have that the above inequality is satisfied if $\beta \geq \frac{ek}{ek + (u-e)(1-M)} \equiv \beta^M$. Average welfare in the monetary equilibrium is given by $W^M = (1 - M) V_0^M + M V_1^M$. It is easy to see that W^M reaches the maximum, \overline{W}^M , when $M = \frac{1}{2}$. In that case, $\overline{W}^M = \frac{u-e}{4k(1-\beta)}$, which is clearly lower than average welfare in the credit equilibrium. ■

The next Lemma asserts that the welfare cost from not being in a credit regime increases in the expected frequency of meetings between two villages. In addition, a sufficient condition is given for credit transactions to be sustainable between two villages.

Intuitively, autarky implies an overall lower expected frequency of consumption. Thus, the higher the frequency of meetings between two villages, the bigger the cost of reverting to no trade. Since punishment becomes more painful, it is easier to support the credit regime. Define $\overline{p}_d \equiv \frac{ek(1-\beta)}{\beta(u-e)}$.

Lemma 2 *Suppose that β is sufficiently high. Consider two villages that are matched with probability p_d . The difference between the value functions under credit and under autarky between them increases in p_d . Furthermore, if $p_d \in (\overline{p}_d, 1)$, all transactions between the two villages use credit, while if $p_d \in (0, \overline{p}_d)$, there is no equilibrium with credit transactions between the two.*

Proof: Consider a distinguished agent from a generic village, j . Let $p^C(p^M)$ be the sum of the matching probabilities with the villages that use credit (money) in meetings

with agents from j . Let p^A be the sum of matching probabilities of the villages that are in autarky with our distinguished agent. Let V_0^C , V_1^C , V_0^A , and V_1^A stand for the value functions under a credit regime and under autarky between our distinguished agent and an arbitrary village j' . These probabilities satisfy $p^C + p^M + p^A + p_d = 1$.

The value functions of our distinguished agent are given by

$$V_0^C = \left(p^C + p_d \right) \left[\beta V_0^C + \frac{1}{k} (u - e) \right] + p^M \left[\left(1 - \frac{1}{k} M \right) \beta V_0^C + \frac{1}{k} M (\beta V_1^C - e) \right] + p^A \beta V_0^C, \quad (3)$$

$$V_1^C = \left(p^C + p_d \right) \left[\beta V_1^C + \frac{1}{k} (u - e) \right] + p^M \left\{ \left[1 - \frac{1}{k} (1 - M) \right] \beta V_1^C + \frac{1}{k} (1 - M) (u + \beta V_0^C) \right\} + p^A \beta V_1^C, \quad (4)$$

and

$$V_0^A = p^C \left[\beta V_0^A + \frac{1}{k} (u - e) \right] + p^M \left[\left(1 - \frac{1}{k} M \right) \beta V_0^A + \frac{1}{k} M (\beta V_1^A - e) \right] + (p^A + p_d) \beta V_0^A, \quad (5)$$

$$V_1^A = p^C \left[\beta V_1^A + \frac{1}{k} (u - e) \right] + p^M \left\{ \begin{array}{l} \left[1 - \frac{1}{k} (1 - M) \right] \beta V_1^A \\ + \frac{1}{k} (1 - M) (u + \beta V_0^A) \end{array} \right\} + (p^A + p_d) \beta V_1^A. \quad (6)$$

In order to support credit transactions between j and j' , we need that $-e + \beta V_0^C \geq \beta V_0^A$ and $-e + \beta V_1^C \geq \beta V_1^A$. It is easy to see that

$$V_1^C - V_1^A = V_0^C - V_0^A = V^C - V^A = \frac{p_d(u - e)}{k(1 - \beta)}, \quad (7)$$

which is clearly increasing in p_d . The expressions for $V_0^C - V_0^A$ and $V_1^C - V_1^A$ are independent of how agents in village j trade in meetings with agents from villages other than j' . Using the first part and substituting $\frac{p_d(u - e)}{k(1 - \beta)}$ for the difference $V^C - V^A$, we have that the conditions that $-e + \beta V_0^C \geq \beta V_0^A$ and $-e + \beta V_1^C \geq \beta V_1^A$ are satisfied

if $p_d \geq \frac{ek(1-\beta)}{\beta(u-e)} \equiv \bar{p}_d$. Notice that \bar{p}_d is decreasing in β . It equals zero when $\beta = 1$ and equals one when $\beta = \beta^C$. ■

It is easy to show that \bar{p}_d increases in k and e , while it decreases in u and β . As the probability of single coincidence becomes smaller, the welfare under a credit regime is reduced. Thus, it becomes harder to support the credit equilibrium. A higher production cost or a lower utility from consumption also makes the credit equilibrium harder to support by reducing the value of consumption. On the other hand, a higher discount factor helps to lower the critical probability.

The previous Lemma does not imply the existence of monetary trades. Producers in meetings where credit cannot be supported, however, will produce in exchange for money provided that acquiring money sufficiently increases their probability of future consumption. This requires that the producers will be able to use their earned money in the near future which, in turn, requires that a meeting with someone from a distant village is likely.

The next Lemma gives sufficient conditions for all transactions in meetings between agents from two villages to be monetary. Let B be the set of villages that are each matched to our generic village, j , with probability less than \bar{p}_d , so that a credit arrangement cannot be supported in meetings between agents from j and any of the villages in B . Let p_B be the probability that village j is matched to a village in B . That is, $p_B = \sum_{d=0}^{\frac{n-1}{2}} p_d$, for $p_d < \bar{p}_d$. Define $\bar{p}_B \equiv \frac{ek(1-\beta)}{\beta(1-M)(u-e)}$.

Lemma 3 *Consider two villages that are matched with probability lower than \bar{p}_d . Provided that $p_B > \bar{p}_B$, there exists an equilibrium where all transactions between the two villages are monetary.*

Proof: For β sufficiently high, a credit equilibrium can be supported in meetings between agents from village j and any village in the complement of B . The value

functions for our distinguished agent can be written as

$$\begin{aligned}
V_1 &= (1 - p_B)[\beta V_1 + \frac{1}{k}(u - e)] \\
&\quad + p_B\{\frac{1}{k}(1 - M)(u + \beta V_0) + [1 - \frac{1}{k}(1 - M)]\beta V_1\} \tag{8}
\end{aligned}$$

$$\begin{aligned}
V_0 &= (1 - p_B)[\beta V_0 + \frac{1}{k}(u - e)] \\
&\quad + p_B[\frac{1}{k}M(-e + \beta V_1) + (1 - \frac{1}{k}M)\beta V_0]. \tag{9}
\end{aligned}$$

For a monetary equilibrium to exist in a meeting between agents from village j and a village $j' \in B$, it is sufficient that $-e + \beta V_1 > 0 + \beta V_0$. Solving for V_0 and V_1 and substituting, we find that the above inequality is satisfied if $p_B \geq \frac{ek(1-\beta)}{\beta(1-M)(u-e)} \equiv \bar{p}_B$. ■

We are ready to state our main Proposition. A credit equilibrium between two villages can be supported if and only if the probability of a meeting between them is greater than \bar{p}_d . In the case where credit is not sustainable, monetary trades may be supported if acquiring money sufficiently increases the probability of consuming in the future; i.e., if a meeting with some other faraway village in the near future is likely.

To better understand the economic principle at work, consider a community of people that trade almost exclusively with residents of the community via the use of credit. Suppose that, in a very unlikely event, one of the residents meets a consumer from far away. It will certainly not be individually optimal to produce for free for the stranger, but what if the stranger offers money in exchange for production? Will the potential producer accept the money and produce? If future meetings are expected to be only with residents of the community, money will be of no use for a long time and will be rejected. On the other hand, if meetings with strangers are frequent enough, the producer can use the money to finance consumption in the near future, and so he will accept it. These observations define the existence of a critical probability that separates the two types of transactions.

Proposition 2 *Suppose that $\beta \in (\beta^C, 1)$. Transactions between village j and villages that are matched to j with probability $p_d \in (\bar{p}_d, 1)$ use credit and, provided that the probability of a meeting between j and a village from B is greater than \bar{p}_B , transactions between j and villages that are matched to j with probability $p_d \in (0, \bar{p}_d)$ are monetary.*

Proof: The sufficient conditions of β to support the credit regime and monetary regime are given in our earlier discussion related to Lemma 1. The existence of a credit regime when $p_d \in (\bar{p}_d, 1)$ and the non-existence of a credit regime when $p_d \in (0, \bar{p}_d)$ follows from Lemma 2. The existence of a monetary regime when $p_d \in (0, \bar{p}_d)$ and $p_B \in (\bar{p}_B, 1)$ follows from Lemma 3. ■

To illustrate this proposition, we present a simple example. Let $u = 8$, $e = 2$, $k = 3$, and $M = 0.5$. Then, $\bar{p}_d = \frac{1-\beta}{\beta}$ and $\bar{p}_B = \frac{2(1-\beta)}{\beta}$. These are plotted in Figure 1. The Figure also demonstrates the regions of values for p_d , p_B , and β , and the equilibria that are supported in these regions. We know that $\bar{p}_d = 1$ implies that $\beta = \beta^C$ and that $\bar{p}_B = 1$ implies that $\beta = \beta^M$. The two vertical lines in Figure 1 give rise to three regions. Consider the generic village j matched with village j' with probability p_d . In region I, autarky is the only equilibrium since the discount factor is too low to support either credit or monetary transactions between the two villages. In region II, if in addition p_d lies above \bar{p}_d , all transactions between j and j' use credit. If p_d lies below, no trade takes place. Monetary transactions cannot be supported in this region since p_B is always less than \bar{p}_B (β is always less than β^M). In region III, if in addition p_d lies above \bar{p}_d , all transactions between j and j' use credit. If p_d lies below, there are two possibilities: autarky or monetary exchange depending on how many other villages lie below \bar{p}_d . If p_B is above \bar{p}_B , transactions between village j and j' are monetary; otherwise autarky prevails. Figure 2 gives the same information regarding region III, in the (p_d, p_B) space.

6. CONCLUSIONS

We studied conditions leading to an equilibrium in which credit is used among agents that meet each other frequently, while money is used in transactions among those that meet only infrequently, in a random matching model. These conditions are that agents meet each other with frequencies that are inversely related to their geographic distance, and that they populate regions that are informationally separated.

It is hard to know the exact form of non-monetized transactions in medieval villages, but observations of contemporary village economies provide some clues. In their study of the financial structure of three villages in India, Lim and Townsend (1998) found evidence consistent with credit functioning well within villages while, at the same time, external credit markets do not function as well, perhaps due to a disadvantage in information sharing.

We emphasize that the local matching rule is necessary for our main result. If we consider our environment under uniform probabilities of matching across all villages, the only possible outcomes would involve either no trade or only credit transactions across all villages, as demonstrated in Section 4. Perhaps the most appropriate interpretation of our model is as a parable of a medieval village economy. Our main proposition suggests that money might emerge when, as a result of increased mobility, trades among people from faraway locations become sufficiently frequent.

In future work we plan to introduce multiple locally-issued fiat objects and study their circulation and redemption properties as a function of the local matching rule. It would also be interesting to study monetary injections and price dispersion in the context of a local interaction model with endogenous prices. In such a model, newly injected money is likely to stay within a small set of locations in the short run. In addition, locally issued money could circulate globally, but at discount that is proportional to the respective distance from the village of issuance.

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8. APPENDIX - VALUE FUNCTIONS

Here we describe the general value functions, special cases of which we used in the paper. We concentrate on the symmetric steady state value function of an agent from a generic village j . We let V_0 and V_1 denote the value function of an agent with and without money, respectively. For the case of an agent with no money, we have

$$V_0 = \sum_{d=0}^{\frac{n-1}{2}} p_d$$

$$\left\{ \left(1 - \frac{2}{k} \right) \beta V_0 + \frac{1}{k} (1 - M) \left[\max_{g_{00}^d} \left(-g_{00}^d h_{00}^d e + \beta V_0 \right) + \max_{h_{00}^d} \left(g_{00}^d h_{00}^d u + \beta V_0 \right) \right] \right\} \\ + \frac{1}{k} M \left\{ \max_{g_{01}^d} \left\{ \begin{array}{l} (1 - m^d) \left(-g_{01}^d h_{01}^d e + \beta V_0 \right) \\ \alpha^d \left(-e + \beta V_1 \right) + g_{01}^d \left(-e + \beta V_0 \right) \\ + \left(1 - \alpha^d - g_{01}^d \right) \beta V_0 \end{array} \right\} \right\} \\ + \max_{h_{10}^d} \left(g_{10}^d h_{10}^d u + \beta V_0 \right) \left. \right\} \quad (\text{A.1})$$

The first part of the value function describes the case of a meeting in which there is no coincidence of wants. The second part describes the case of a single coincidence meeting as a producer and as a consumer, respectively, with an agent that has no money holdings. In that case, our distinguished agent chooses whether to offer credit and whether to receive credit, respectively. Finally, the third part describes the case of a single coincidence meeting as a producer and as a consumer, respectively, with an agent that has money. In that case, our distinguished agent chooses whether to offer credit or to offer to produce in exchange for his partner's money holdings, etc. Similarly, for the case of a distinguished agent with money, we have

$$V_1 = \sum_{d=0}^{\frac{n-1}{2}} p_d$$

$$\left\{ \left(1 - \frac{2}{k} \right) \beta V_1 + \frac{1}{k} M \left[\max_{g_{11}^d} \left(-g_{11}^d h_{11}^d e + \beta V_1 \right) + \max_{h_{11}^d} \left(g_{11}^d h_{11}^d u + \beta V_1 \right) \right] \right\} \\ + \frac{1}{k} (1 - M) \left\{ \max_{g_{10}^d} \left(-g_{10}^d h_{10}^d e + \beta V_1 \right) \right. \\ \left. + \max_{m^d} \left\{ \begin{array}{l} (1 - m^d) \left[\max_{h_{01}^d} \left(g_{01}^d h_{01}^d u + \beta V_1 \right) \right] \\ \alpha^d \left(u + \beta V_0 \right) + g_{01}^d \left(u + \beta V_1 \right) \\ + \left(1 - \alpha^d - g_{01}^d \right) \beta V_1 \end{array} \right\} \right\} \left. \right\} \quad (\text{A.2})$$

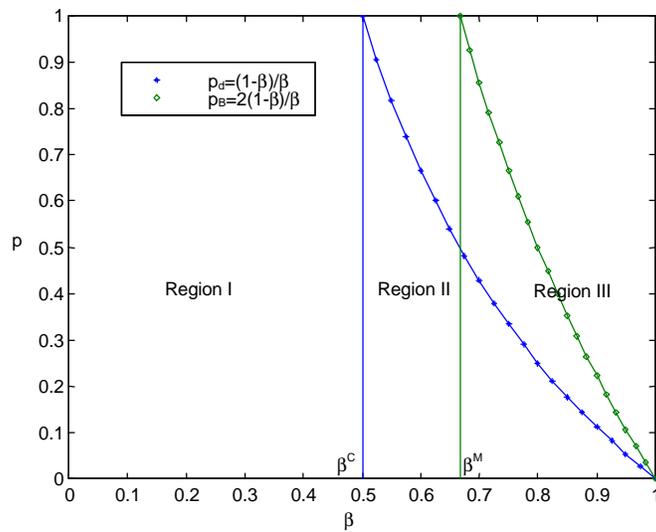


FIG. 1. Regions for p_d , p_B , β and Equilibria

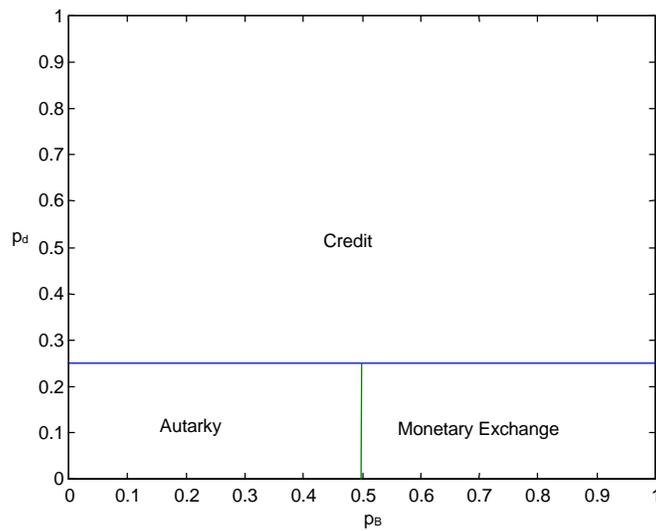


FIG. 2. Regions for p_d , p_B and Equilibria, $\beta = 0.8$